Experimental and numerical investigation of plywood progressive failure in CT tests

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Abstract: The plywood is considered as a layered cross-ply unidirectional fibre reinforced composite. The experimental Compact Tension (CT) tests carried out in different directions of plywood fibre orientation show that the characteristics of damages are fibre bundle rupture, matrix cracking along the fibres, and delamination at the ply interlayers of glue. The plywood CT specimens are modelled by continuum shell and cohesive finite elements with damage evolution in material models. The Finite Element (FE) model simulates the experimental behaviour of plywood samples very well and allows deep investigation of the different types of damage development and interaction. The FE model of plywood is useful for its lay-up optimization and for development of very efficient in large-scale simulations computational models of plywood.

Key words: plywood, veneer, progressive failure, damage, finite element model, finite element simulation.

1. Introduction

Plywood is very popular material in civil engineering and furniture industry, because it is comparatively cheap, strong, and lightweight material. Its strength and progressive failure resistance are very important for wooden houses survivability in earthquake, tornado, and hurricane events [1-3]. The progressive failure of plywood, however, is complicated because of its structure as a layered natural composite which is very similar to polymeric unidirectional fibre reinforced composites.

Plywood is made from thin sheets of timber – veneer, called also plies. The timber is orthotropic fibre material with well pronounced difference in elastic and mechanical properties between the longitudinal (L) to the fibres direction and the tangential direction (T) to the annually growth rings. The veneers are cut by rotating the trunks and therefore they are oriented in the LT-plane of timber material with a normal in radial (R) direction of the log. They are stacked together with the fibre direction of each ply perpendicular to the fibre direction of its adjacent ones and usually the plywood has an odd number of plies. The veneers are bonded together
under heat and pressure with strong adhesive, which makes the plywood a type of layered composite material. Plywood is used in many applications as a lumber of a higher quality because of its resistance to cracking, breaking, twisting and warping although the pure wood is very brittle material.

The Finite Element (FE) method was developed in recent few decades as a superior numerical method that could produce computer simulations of different phenomena of the real world. This allows many researchers to use the FE technique to investigate some problem that is not easy to be directly observed and its parameters to be measured. The FE method is best developed for Solid and Structure mechanics and it is enriched with many material models, including damage models as well as specific structure finite elements like cohesive elements, continuum shell elements, etc.

In this paper the problem of progressive failure in plywood material is investigated by Compact Tension (CT) experimental tests and FE analysis. The plywood specimens are made from spruce and pine veneers. The gradual degradation and fracture process of this material is very complicated. It obeys both description of damage growth in plies and delamination of composite layers. The numerical simulation of the problem was done by application of FE technique and ABAQUS™ commercial code.

2. Experimental CT tests of plywood

Compact Tension (CT) tests of 9-ply plywood were conducted using three types of specimens shown in Fig. 1: (a) with fibres of the outer plies oriented in the direction of loading, (b) with fibres of the outer plies oriented perpendicular to the direction of loading, and (c) with fibres in bias direction (45°) to the loading direction. Taking the outer plies as reference plies, the specimens can be denoted as longitudinal, transverse, and bias samples, respectively.

Fig. 1. Compact tension specimens of plywood with different orientation.

The longitudinal specimens with the fibres of the outer plies oriented in the loading direction failed with non even edges for these plies caused by fibre bundle rupture at different places along the fibres (see Fig. 2). The plies have cracks along the fibres connecting the different places of bundle rupture. The force developed and the displacement of the grips are registered for appropriate match of FE simulation to the experimental tests.
The transverse specimens failed with even failure edge of outer plies, having fibres oriented perpendicular to the loading direction, which could be seen in Fig. 3. The failure of outer plies is cracking along the fibres. The internal plies of the transverse specimens as well as of the longitudinal ones have very similar modes of failure as the outer plies depending on their orientation to the loading direction. Because the places of failure of the adjacent plies are different, the ruptured fibre bundles are pulled out after delamination at the glued interlayer connecting the plies.

When the bias specimens are tested, the fracture edges of the different layers are not straight lines (see Fig. 4). They are zigzag lines that possess the characteristics of failure of both – failure of the longitudinal to the loading direction plies and failure of the transverse plies. We have some fibre-bundles ruptured and comparatively long cracks along the fibres connecting the places of bundle rupture. The lines of failure of the different plies, however, do not coincide and delamination accompanies the failure.
Fig. 4. Failure of a bias CT specimen.

All specimens of plywood in CT tests have delamination between the layers, independently of the orientation of the fibres. Adjacent layers have failure at different places because of their different fibre orientation. This causes delamination, which is ply interface failure in shear, in fact, with fibres pulled out and formation of pockets as it could be seen in Fig. 5.

Fig. 5. Close look of the plywood failure area.

3. Finite element model of plywood

In order to simulate properly the progressive failure of plywood in tension, we need to have good models of the mechanical behaviour of its constituents. The veneers are orthotropic sheet material with very brittle behaviour. Their structure in mesoscale level consists of tubular water-conducting elements (tracheids) which are stronger in their longitudinal direction and weaker in transverse direction [4]. In microscopic level, the walls of tracheids are built up of long cells having unidirectional fibres of cellulosic along the tracheids, which are connected together by lignin.
3.1. Single veneer model

The best choice for us is to represent the veneer as a unidirectional fibre composite layer with orthotropic elastic properties and damage evolution. ABAQUS™ finite element code has a readily available damage model for unidirectional fibre composites and 2-D stress elements [5]. The material model can be used with the proper material and mechanical data for continuum shell elements in which each ply is discretized.

Damage variables, $d_f$, $d_m$ and $d_s$, degrade the elastic moduli of material $E_L$, $E_T$ and $G_{LT}$ in the damaged elasticity matrix $C_d$:

$$
C_d = \begin{pmatrix}
    c_{11} & c_{12} & 0 \\
    c_{12} & c_{22} & 0 \\
    0 & 0 & c_{33}
\end{pmatrix}
$$

where

$$
c_{11} = (1 - d_f)E_L / D
$$

$$
c_{12} = (1 - d_f)(1 - d_m)\nu_{LT}E_T / D
$$

$$
c_{22} = (1 - d_m)E_T / D
$$

$$
c_{33} = (1 - d_s)G_{LT}
$$

$$
D = 1 - (1 - d_f)(1 - d_m)\nu_{LT}^2 E_T / E_L
$$

The damaged elasticity matrix governs the material constitutive equation:

$$
\sigma = C_d \cdot \varepsilon
$$

where $\sigma = [\sigma_L \quad \sigma_T \quad \tau_{LT}]^T$ is 2-D stress vector, corresponding to 2-D strain vector $\varepsilon = [\varepsilon_L \quad \varepsilon_T \quad \gamma_{LT}]^T$.

The damage variable, $d_f$, is determined by two modes of damage (fibre breakage) in dependence of the applied loading in fibre direction – tension or compression:

$$
d_f = \begin{cases}
    d_p, & \sigma_L \geq 0 \quad \text{fibre rupture} \\
    d_k, & \sigma_L < 0 \quad \text{fibre kinking}
\end{cases}
$$

while the damage variable, $d_m$, is determined by other two modes of matrix damage:

$$
d_m = \begin{cases}
    d_{mt}, & \sigma_T \geq 0 \quad \text{matrix cracking} \\
    d_{mc}, & \sigma_T < 0 \quad \text{matrix crushing}
\end{cases}
$$

These modes are independent and could be generally denoted by index $M$. The shear damage variable, $d_s$, is resultant of all four independent damage modes:
The independent damage variables are initially zero and their evolution could begin when the corresponding failure criterion for damage initiation, $F_M$, becomes greater than unity ($F_M > 1$). The failure criteria of Hashin and Rotem [6] for each mode are as follows:

$$F_{ft} = \left( \frac{\sigma_L}{X_T} \right)^2$$

(11)

$$F_{fc} = \left( \frac{\sigma_L}{X_C} \right)^2$$

(12)

$$F_{mt} = \left( \frac{\sigma_T}{Y_T} \right)^2 + \left( \frac{\tau_{LT}}{S_{LT}} \right)^2$$

(13)

$$F_{mc} = \left( \frac{\sigma_T}{2S_{RT}} \right)^2 + \left( \frac{Y_C}{2S_{RT}} \right)^2 - 1 \left( \frac{\sigma_T}{Y_C} + \left( \frac{\tau_{LT}}{S_{LT}} \right)^2 \right)$$

(14)

where $X_T$ is the strength of veneer in tension in longitudinal ($L$) direction, $X_C$ – compressive strength in $L$-direction, $Y_T$ – tensile strength in tangential ($T$) direction, $Y_C$ – compressive strength in $T$-direction, $S_{LT}$ – in-plane shear strength, $S_{RT}$ – transverse shear strength.

The degradation of the stiffness of the material could cause several numerical problems in the calculations. First of all, a regularization procedure should be applied, in order to avoid the strain localization in one finite element and the sever mesh dependence of the simulation. The regularization procedure here is that the damage model is applied as a local damage, i.e. the damage evolution law is in term of equivalent displacements, not in strains. A characteristic length $L_C$ is prescribe for each element in order to calculate the equivalent displacement, $\delta_{eq}^\text{eq}$, determining the damage evolution for each independent damage mode, $M$, after the damage initiation of the mode. The equivalent displacement is calculated for the fiber breakage modes simply by the formula:

$$\delta_{eq}^\text{eq} = L_C \sqrt{\varepsilon_L^2}$$

(15)

and for matrix damage modes by:

$$\delta_{eq}^\text{eq} = L_C \sqrt{\varepsilon_T^2 + \gamma_{LT}^2}$$

(16)

The static damage variable, $d_M$, for each active mode $M$ is calculated by an irreversible linear-softening damage evolution law:

$$d_M^\text{eq} = \max \left\{ d_M^\text{st}, \frac{\delta_M^\text{eq} (\delta_M^\text{eq} - \delta_M^\text{lim})}{\delta_M^\text{eq} (\delta_M^\text{eq} - \delta_M^\text{lim})} \right\}$$

(17)
where $\delta_{\text{lim}}^M$ is the equivalent displacement for mode $M$ calculated exactly when the damage initiation for this mode is satisfied by the corresponding criterion ($\delta_{\text{lim}}^M = \delta_{\text{eq}}^M$). $\delta_{\text{ult}}^M$ is the ultimate equivalent displacement that could be reached in dependence of the dissipated fracture energy, $G_M^{\text{cr}}$, for this mode of damage:

$$\delta_{\text{ult}}^M = 2 \frac{G_M^{\text{cr}}}{\sigma_{\text{eq}}^M}$$

(18)

Here, $\sigma_{\text{lim}}^M$ is the equivalent stress for mode $M$ exactly when the damage initiation criterion for this mode is satisfied ($\sigma_{\text{lim}}^M = \sigma_{\text{eq}}^M$) and these equivalent stresses of the damage modes, $\sigma_{\text{eq}}^M$, are calculated as follows:

$$\sigma_{\text{eq}}^M = \begin{cases} |\sigma_L|, & M = ft, fc \\ \frac{\sigma_T \varepsilon_T + \tau_{LT} \gamma_{LT}}{\delta_M / L_c}, & M = mt, mc \end{cases}$$

(19)

The evolution of damage variables is graphically explained by equivalent stress-displacement diagram in Fig. 6. The material is linearly elastic for any mode of damage until the damage initiation (failure) criterion for this mode is met – ascending branch. When the damage is already initiated and the equivalent displacement, $\delta_{\text{eq}}^M$, is greater than the limit, $\delta_{\text{eq}}^M > \delta_{\text{lim}}^M$, the static damage variable is calculated ($d_m^M \in [0, 1]$) to reduce the equivalent stress, $\sigma_{\text{eq}}^M$, linearly by multiplier $(1 - d_m^M)$ (descending branch) in such a way that the totally dissipated energy up to the ultimate failure, when equivalent displacement reaches the ultimate displacement, $\delta_{\text{ult}}^M$, to be the critical fracture energy for this mode, $G_M^{\text{cr}}$, representing the gray area of the triangle. Any unloading will retain the damage variable constant until the successive loading reaches the last point of unloading (the thin line with arrows).

Fig. 6. Irreversible linear softening damage evolution.

Since the descending branch of stress development represents a negative tangential stiffness of the material and therefore unstable solution for nonlinear static problems, the stabilization procedure is necessary to provide computationally efficient solution. The method that is applied here is a viscous damping and the damage variable for each independent damage mode, degrading the damaged elastic matrix, is calculated as solution of the time dependent differential equation:
\[ \dot{d}_M = \frac{1}{\eta_M}(d_M^{eq} - d_M), \]  

where \( \eta_M \) is the viscous coefficient for this mode of damage \( M \).

Fig. 7. Single veneer specimen in longitudinal (L) tension: (a) experimental failure, (b) fibre rupture damage, (c) matrix cracking damage.

Fig. 8. Single veneer specimen in transverse (T) tension: (a) experimental failure, (b) matrix cracking damage.

Fig. 9. Single veneer specimen in bias (45°) tension: (a) experimental failure, (b) matrix cracking damage.
In order to find the elastic and mechanical properties of single veneer, three types of specimens of pine and spruce wood were prepared with different orientation of fibres in the direction of loading. The tension tests were conducted in longitudinal, transverse, and bias (45°) direction to the direction of fibres of the specimens. The specimen of single veneer for tension tests is modelled by continuum shell finite elements in ABAQUS™ software. The damage model described above is used for material model. The elastic and mechanical properties of the material for continuum shell elements are tuned in order to obtain force-displacement curve, which is as close as possible to the experimental one with its breaking point at the maximum force reached.

A typical failure of specimens in longitudinal to their fibres tension is shown in Fig. 7a. The fracture edge of specimen is not even because the fibres are ruptured in bundles at different places and they are connected by cracks along the fibres [7]. The damages that appear in longitudinal tension simulations are not only fibre rupture Fig. 7b but also matrix cracking Fig. 7c. This very well corresponds to the experimental observations although, because of the symmetric regular mesh, the simulations are perfect and they show symmetrically developed damage starting from four points of the specimen model while, in reality, the heterogeneity and imperfection cause unsymmetrical damage development.

The results for specimens in tension in transverse to the fibres direction are given in Fig. 8. The picture in Fig. 8a shows very even edge of fracture since the specimen is split along the fibres [4, 8]. The simulations show only matrix cracking mode of damage, which appear in a strip perpendicular to the loading direction as can be seen in Fig. 8b.

The results for tension in bias direction are similar to those of transverse direction (Fig. 9). The fracture edge is again even, but in 45 degree to the direction of tension as the specimens are split along the fibres (Fig. 9a). The FE simulations show the same damage mode but, because of the regular mesh and perfect material, the damage starts to develop from two points of the specimen and advances in 45° to the loading direction (Fig. 9b).

The average curve of each direction of tension tests represents the elastic property of veneer in the given direction of loading. The elastic properties of the veneer material are tuned in such a way in order to simulate elastic behaviour of the specimen negotiating the average force-displacement curve obtained in experiments for the given loading. The results of tuning the elastic properties by simulations are given in Tab. 1 for the two types of wood veneer.

Table 1. Elastic properties of single veneers of different type of wood.

<table>
<thead>
<tr>
<th>Wood</th>
<th>$E_L$ (MPa)</th>
<th>$E_T$ (MPa)</th>
<th>$\nu_{LT}$ (–)</th>
<th>$G_{LT}$ (MPa)</th>
<th>$G_{LR}$ (MPa)</th>
<th>$G_{RT}$ (MPa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>pine</td>
<td>6300</td>
<td>130</td>
<td>0.51</td>
<td>350</td>
<td>200</td>
<td>50</td>
</tr>
<tr>
<td>spruce</td>
<td>6200</td>
<td>210</td>
<td>0.013</td>
<td>350</td>
<td>200</td>
<td>40</td>
</tr>
</tbody>
</table>

The strength properties of the material, determining the damage initiation, are tuned in order to give maximum forces in force-displacement diagrams for pine and spruce veneers. As a result of the strength adjustment together with the fracture energy tuning [9], in order to have proper descending branch of the diagrams, the mechanical properties of all three types of single veneer wood are determined and given in Tab. 2 as parameters of the damage model accepted here for the numerical simulations. The
maximum breaking forces obtained in the simulations are given in Tab. 3 for comparison with the experimental average. The maximum force obtained in the simulations is very close to that in the experiment excluding the case of bias tension, in which the maximum force is lower than the experimental one for both types of wood.

Table 2. Mechanical properties of single veneers of different type of wood.

<table>
<thead>
<tr>
<th>Wood</th>
<th>TX (MPa)</th>
<th>CX (MPa)</th>
<th>TY (MPa)</th>
<th>CY (MPa)</th>
<th>LTS (MPa)</th>
<th>TRS (MPa)</th>
<th>cr (N/mm)</th>
<th>G (N/mm)</th>
<th>mc (N/mm)</th>
<th>mt (N/mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>pine</td>
<td>26.7</td>
<td>20</td>
<td>0.8</td>
<td>10</td>
<td>12</td>
<td>12</td>
<td>0.98</td>
<td>0.98</td>
<td>0.03</td>
<td>0.10</td>
</tr>
<tr>
<td>spruce</td>
<td>78.0</td>
<td>50</td>
<td>2.2</td>
<td>10</td>
<td>20</td>
<td>20</td>
<td>1.6</td>
<td>1.6</td>
<td>0.06</td>
<td>0.20</td>
</tr>
</tbody>
</table>

Table 3. Maximum breaking force match between experimental tests and simulations.

<table>
<thead>
<tr>
<th>Wood</th>
<th>Direction</th>
<th>Experimental Average</th>
<th>FE Simulations</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>displacement (mm)</td>
</tr>
<tr>
<td>pine</td>
<td>longitudinal</td>
<td>0.69</td>
<td>689.1</td>
</tr>
<tr>
<td></td>
<td>transverse</td>
<td>0.94</td>
<td>20.0</td>
</tr>
<tr>
<td></td>
<td>bias</td>
<td>0.78</td>
<td>53.0</td>
</tr>
<tr>
<td>spruce</td>
<td>longitudinal</td>
<td>1.71</td>
<td>1755</td>
</tr>
<tr>
<td></td>
<td>transverse</td>
<td>1.59</td>
<td>55.9</td>
</tr>
<tr>
<td></td>
<td>bias</td>
<td>1.42</td>
<td>122.1</td>
</tr>
</tbody>
</table>

The agreement between the experimental and the simulated by FE method behaviour of single veneer is very good, which is a basis for representative FE analysis of plywood progressive failure. Of course, we need to simulate the interface failure between the plies, which causes delamination of the plywood at some stage of the progressive failure.

3.2. Interlayer failure and delamination

Specimens of 5-ply plywood are prepared with notches deep to the middle ply and at 8 mm distance as it is shown on the photograph in Fig. 10a. The tension of both ends of the specimens causes shear and something like delamination of the plies. The fracture usually happens near the one of the interfaces of the middle ply with one of its adjacent ply, as it is shown in Fig. 10b. The surface of fracture however is not exactly the glued surface. Some of the material of the adjacent layer is stuck on the middle ply (Fig. 10c).

Fig. 10. Plywood specimen tested in shear.
The results of shear tests are used to set the strength of ply interface [10], which can be simulated in FE model of plywood by cohesive elements. They are very similar to continuum shell elements in their geometry and nodal degrees of freedom. 3-D elements have three translational degrees of freedom per node and local coordinate system defining the normal of the element and two tangential directions in the plane of the element.

The constitutive response of cohesive elements is determined by traction-separation relationship [5]. The separation in cohesive elements is defined as a relative displacement of upper nodes to lower nodes with respect to their normals with three components: \( \delta_i \), \( i = n, s, t \) in normal direction, \( n \), and in the other two tangential directions, \( s \) and \( t \), respectively. Using the element thickness, \( h \), the constitutive response of damaged element can be defined as:

\[
T_i = (1 - d_i) \frac{K^{(i)}}{h} \delta_i \quad \text{(no summation on } i) \tag{21}
\]

where \( T_i \) are the traction components and \( d_i \) is a damage variable which is initially zero and when the damage initiation criterion is met it could has evolution and could reach unity.

The damage initiation is determined by quadratic nominal stress criterion:

\[
F_c = \left( \frac{T_n}{\sigma_{\text{lim}}} \right)^2 + \frac{T_s^2 + T_t^2}{(\tau_{\text{lim}})^2} \tag{22}
\]

when it becomes greater than unity \( F_c \geq 1 \). Here \( \sigma_{\text{lim}} \) and \( \tau_{\text{lim}} \) are the peeling and shear strengths of the interface while the symbol \( \left[ \right] \) denotes Macaulay’s brackets.

Effective traction, \( T_{\text{eff}} \), and effective separation, \( \delta_{\text{eff}} \), are calculated at the initiation of damage:

\[
T_{\text{eff}} = \sqrt{T_n^2 + T_s^2 + T_t^2} \tag{23}
\]

\[
\delta_{\text{eff}} = \sqrt{\delta_n^2 + \delta_s^2 + \delta_t^2} \tag{24}
\]

and they are denoted as \( T_{\text{lim}} \) and \( \delta_{\text{lim}} \), respectively.

The damage evolution after the damage initiation is governed by linear softening, which can determined the static damage variable, \( d_{\text{st}} \), by the expression:

\[
d_{\text{st}} = \max \left\{ d_{\text{st}}^0, \frac{\delta_{\text{eff}} (\delta_{\text{eff}} - \delta_{\text{lim}})}{\delta_{\text{eff}} (\delta_{\text{st}} - \delta_{\text{lim}})} \right\} \tag{25}
\]

where \( \delta_{\text{eff}} = 2G_{\text{cr}} / T_{\text{eff}} \) is the ultimate effective separation calculated from critical fracture energy of cohesion, \( G_{\text{cr}} \). The damage evolution in cohesive elements is very similar to the single veneer damage evolution and it can be illustrated by the diagram in Fig. 6 replacing equivalent displacement and stress by effective separation and traction. The total critical fracture energy is defined by its three components:
\[ G_{cr}^{ct} = G_{n}^{cr} + G_{s}^{cr} + G_{t}^{cr} \]  

and in the mix-mode failure at the ultimate state the components of the dissipated energy satisfy the power law criterion:

\[
\left( \frac{G_{n}}{G_{cr}^{n}} \right)^{\alpha} + \left( \frac{G_{s}}{G_{cr}^{s}} \right)^{\alpha} + \left( \frac{G_{t}}{G_{cr}^{t}} \right)^{\alpha} = 1
\]

with parameter \( \alpha = 2 \) in this case. When the cohesive elements are used to connect continuum shell elements, they are not loaded by peeling traction and the only mode of failure of cohesive elements is shear.

In order to avoid numerical difficulties in FE simulation of cohesive elements failure, viscous damage stabilization is implemented. The viscous damage variable, \( d_c \), degrading the elastic properties of material, is calculated from the static damage variable, \( d_c^{st} \), using the viscous coefficient \( \eta_c \) by the relationship:

\[
\dot{d}_c = \frac{1}{\eta_c} (d_c^{st} - d_c)
\]

The accepted properties of cohesive elements and their failure parameters are chosen to correspond to the shear strength determined experimentally and to some data found in literature. The properties are given in Tab. 4. The thickness of the cohesive elements used in the FE model of plywood is very small, it is \( h = 0.02 \) mm. In order to have stable calculation when the cohesive element properties are degraded, viscous stabilization is accepted for cohesive elements with viscous coefficient \( \eta_c = 0.01 \) s.

Table 4. Properties of cohesive elements modeling the plywood interlayer connection.

<table>
<thead>
<tr>
<th>( K_n ) (MPa)</th>
<th>( K_s ) (MPa)</th>
<th>( K_t ) (MPa)</th>
<th>( \sigma_n^{lim} ) (MPa)</th>
<th>( \sigma_s^{lim} ) (MPa)</th>
<th>( \sigma_t^{lim} ) (MPa)</th>
<th>( G_n^{cr} ) (N/mm)</th>
<th>( G_s^{cr} ) (N/mm)</th>
<th>( G_t^{cr} ) (N/mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1910</td>
<td>250</td>
<td>250</td>
<td>20</td>
<td>6.89</td>
<td>6.89</td>
<td>0.6</td>
<td>0.6</td>
<td>0.6</td>
</tr>
</tbody>
</table>

4. CT test simulations and results

A quarter of plywood CT specimen was modelled by finite elements. Each veneer ply is modelled by one layer of continuum shell elements. The layers are connected by one interlayer of cohesive elements with 0.02 mm thickness. The plies of veneer have thickness of 1.5 mm and the continuum shell elements account for this thickness by deducting the thickness of cohesive elements from it in order to obey the total thickness of the plywood. The lay-up is set to [pine/spruce/spruce/pine/pine].

The loading velocity in the CT test simulations is 1 mm/s and the viscous coefficients for stabilization, which are used in the damage model of continuum shell elements as well as in cohesive elements, are all equal to 0.01 s.

The simulation of longitudinal CT specimens in tension gave force-displacement curve, which is given in Fig. 11a in comparison with the experimental ones of three specimens. The maximum breaking force in the simulation is in good agreement with the experimental average but the descending branch is not steep enough.
and damages in the simulation are delayed. The simulation of transverse CT specimens in tension shows very similar results as force-displacement curve, which is given in Fig. 11b. The force-displacement curve of simulated bias tension is lower than the experimental ones (see Fig. 11c). The maximum breaking forces of single veneer tension in this direction, however, are lower than the experimental averages for both pine and spruce wood and this explains the results.

Fig. 11. Force-displacement diagrams of three specimens compared with the simulation.
The contour plots shown in Fig. 12 are taken for the same instant of longitudinal tension simulation. They present the development of fibre rupture damage in longitudinal plies (Fig. 12a) which advances, except in the stronger spruce wood veneer, followed almost immediately by the matrix cracking of transverse plies (Fig. 12b) and then followed with some delay by the delamination of interlayers (Fig. 12c).

The contour plots shown in Fig. 13 present the development of matrix cracking of transverse plies (Fig. 13a) together with fibre rupture damage in longitudinal plies (Fig. 13b), which advances in the weaker pine wood ply and delayed in the stronger veneer. The matrix cracking of transverse plies is like more pronounced here in comparison with the longitudinal sample and the delamination of the interlayers (Fig. 13c) is again delayed.

Fig. 12. Damages in longitudinal tension: (a) fibre rupture in longitudinal layers, (b) matrix cracking in transverse layers, (c) delamination in interlayers.
Fig. 13. Damages in transverse tension: (a) matrix cracking in transverse layers, (b) fiber rupture in longitudinal layers, (c) delamination in interlayers.

The contour plots of damages in bias tension of plywood show that the fibre rupture is very delayed and the main damage mode of material failure is the matrix cracking of all plies shown in Fig. 14a. This damage however, is advanced by the delamination between the plies (see Fig. 14b). In this type of loading the delamination appears to play significant role. It is well known that the shear of material is the main failure in bias loading of layered fibre reinforced composites.

Fig. 14. Damages in bias tension: (a) matrix cracking in all layers, (b) delamination in interlayers.
5. Conclusions

The FE model of plywood seems to represent qualitatively the progressive failure in CT tests very well. The model needs some amendments maybe to improve its quantitative representation. The force-displacement curves of simulations do not correspond very well to the experimental ones. The higher delay of damage development in the simulations is maybe due to the higher viscous coefficient for calculation stabilization as well as to the higher critical fracture energies of some damage modes or cohesive element failure.

The FE model of plywood offer good qualitative results and it is capable to be used for progressive failure investigation giving better understanding of this complex process. The FE model can be utilized for optimization of plywood lay-up to reach higher strength. The model is computationally efficient enough for CT test simulations but not for large-scale structure simulations. The model is useful, however, for developing more efficient model of the layered composite with delamination for large-scale simulations as a basis for comparison.

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