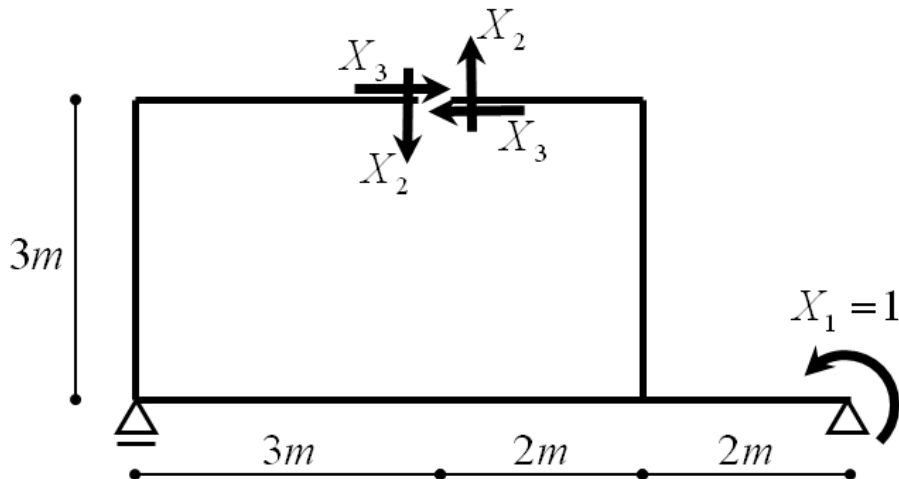


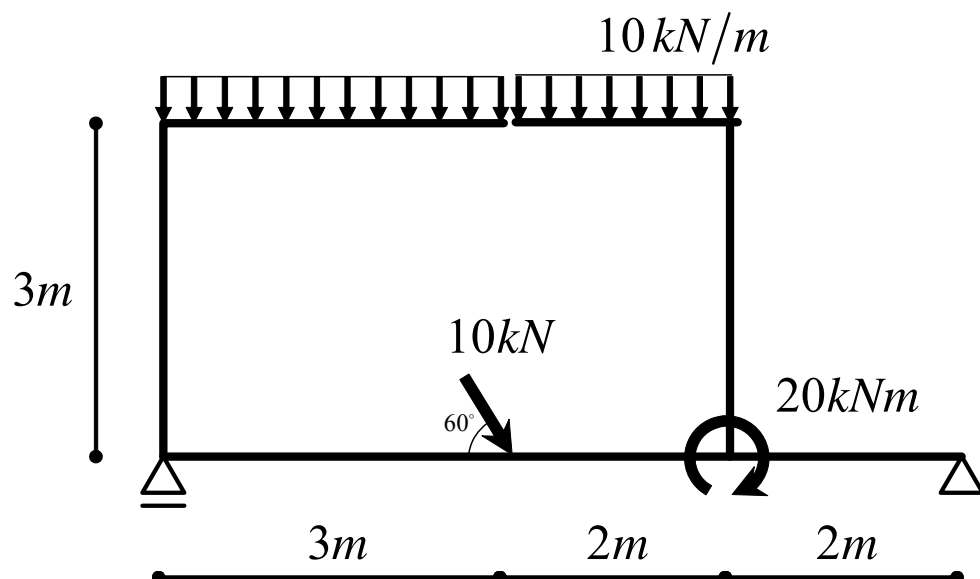
$$E = 205 \text{ GPa} \quad \alpha_t = 1.2 \cdot 10^{-5} \cdot \frac{1}{\text{K}}$$

$$\text{Przekrój: I200} \quad h = 0.2 \text{ m} \quad I_x = 2140 \text{ cm}^4 \quad E \cdot I_x = 4387 \cdot \text{kN} \cdot \text{m}^2$$

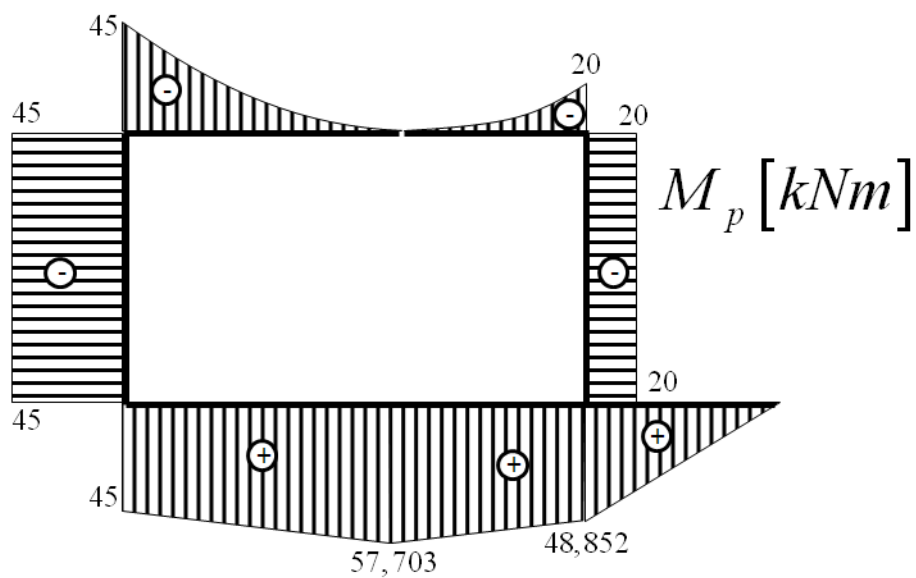
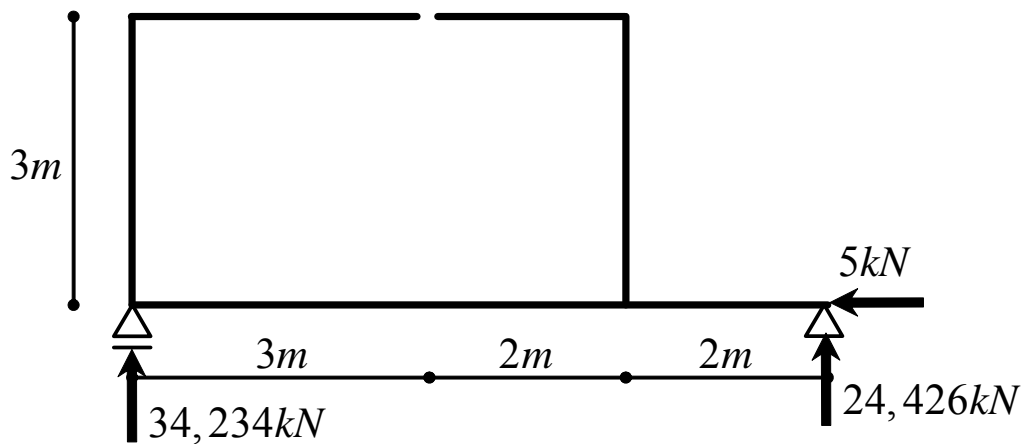
### Układ podstawowy metody sił (UPMS)



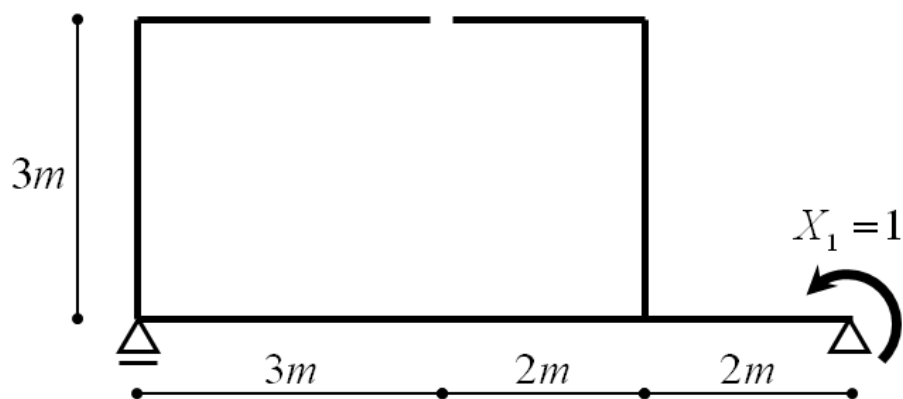
### Stan "p"



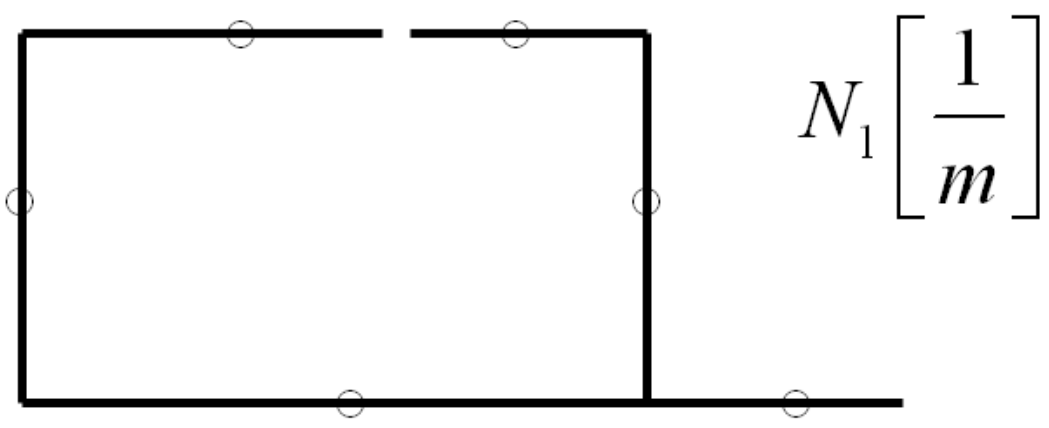
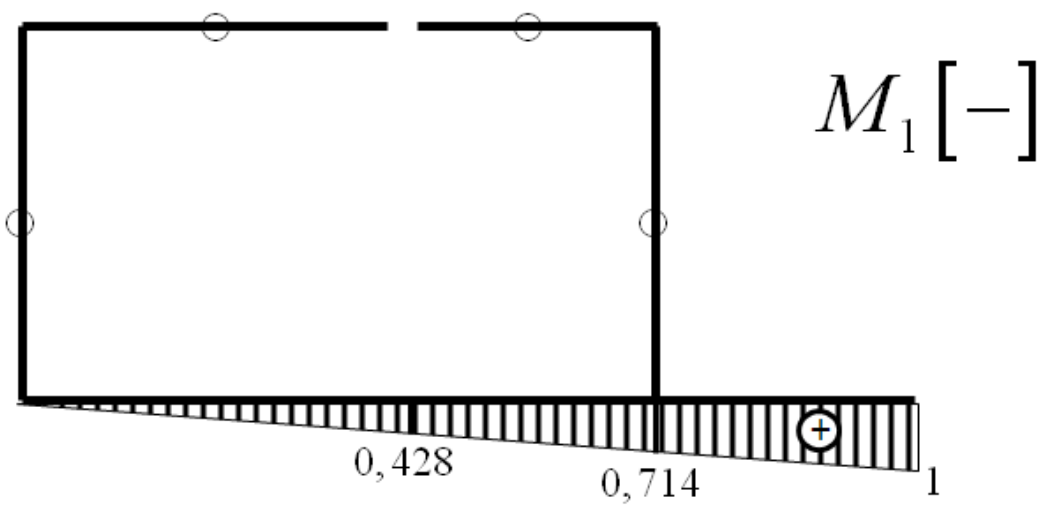
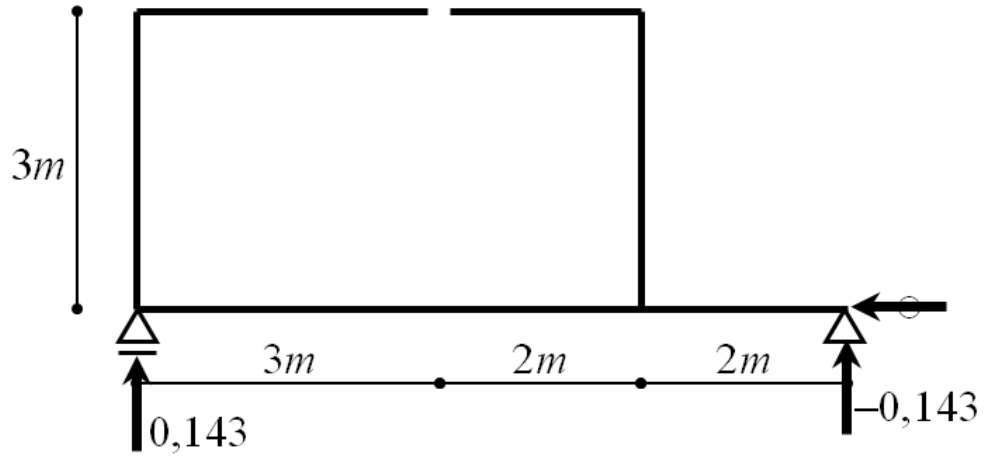
### Reakcje w stanie "p"



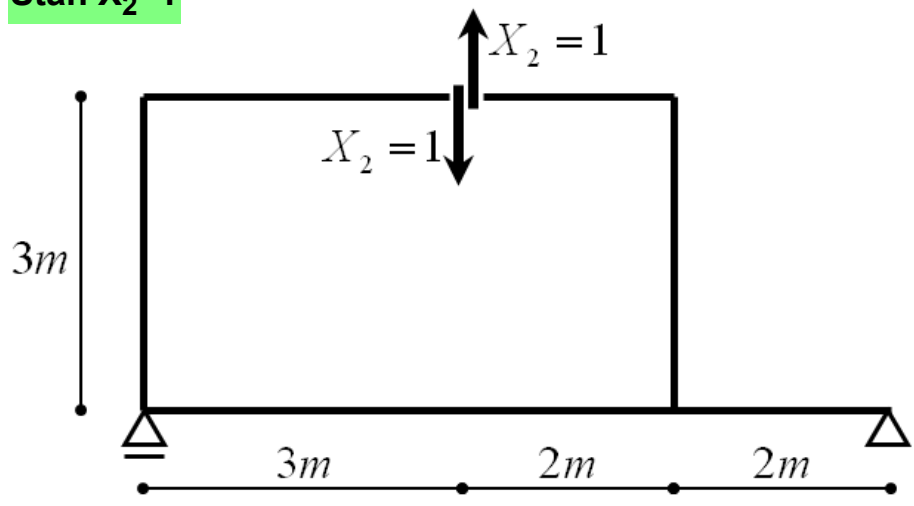
### Stan $X_1=1$



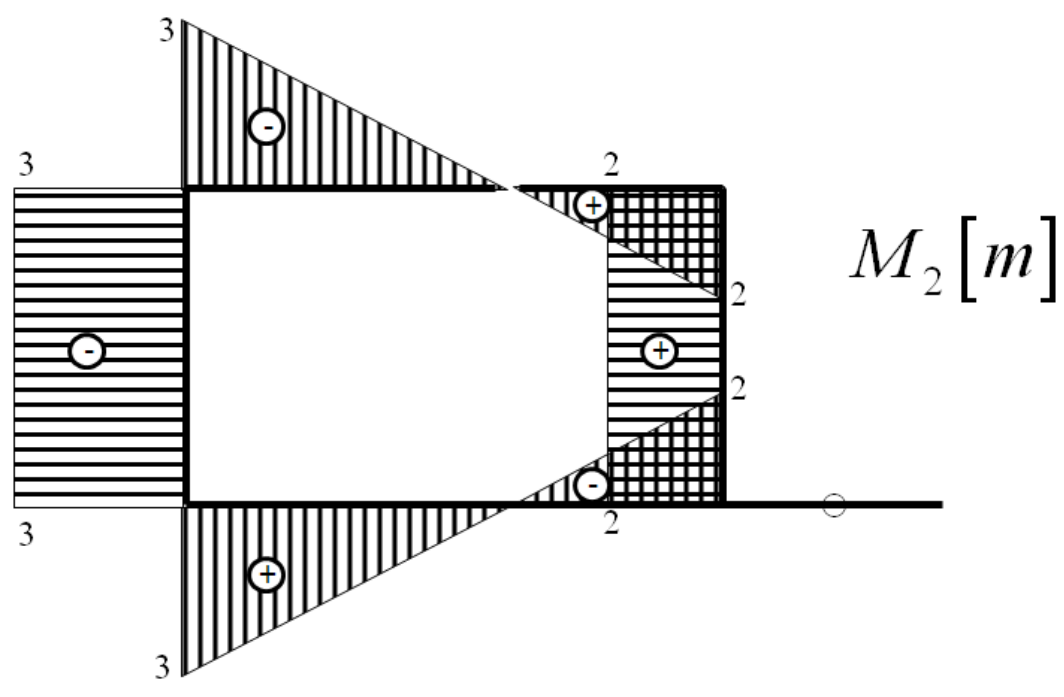
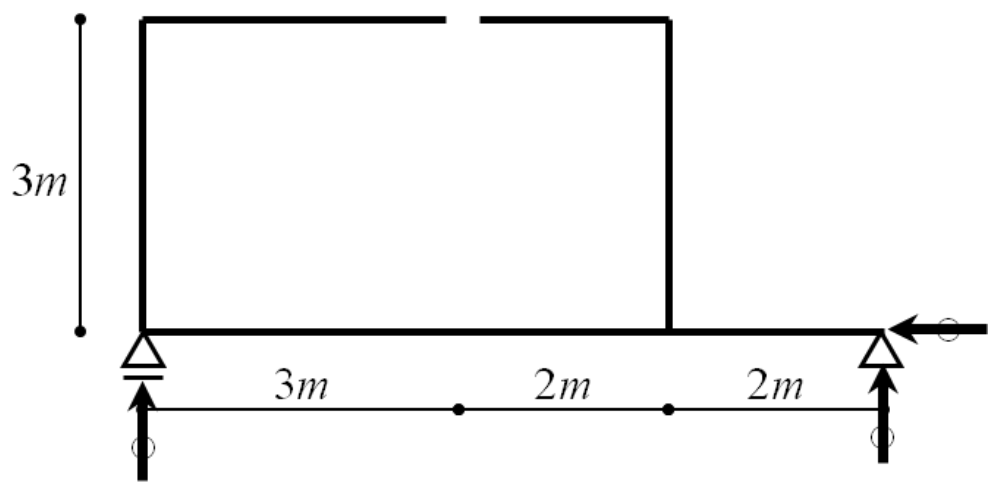
Reakcje w stanie  $X_1=1$

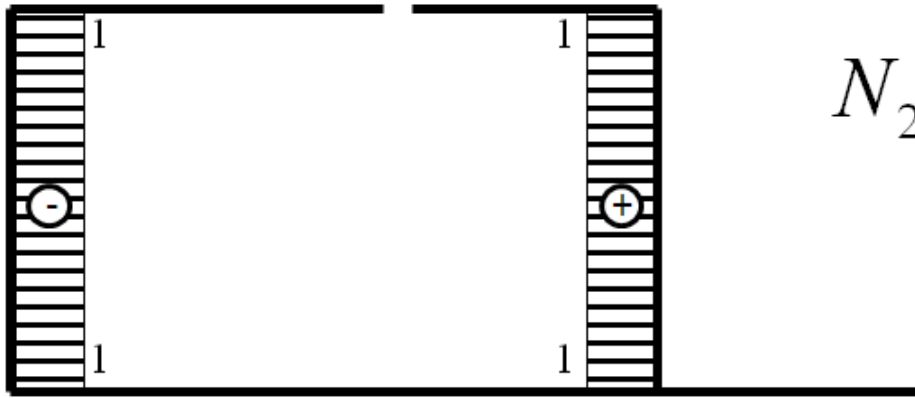


Stan  $X_2=1$



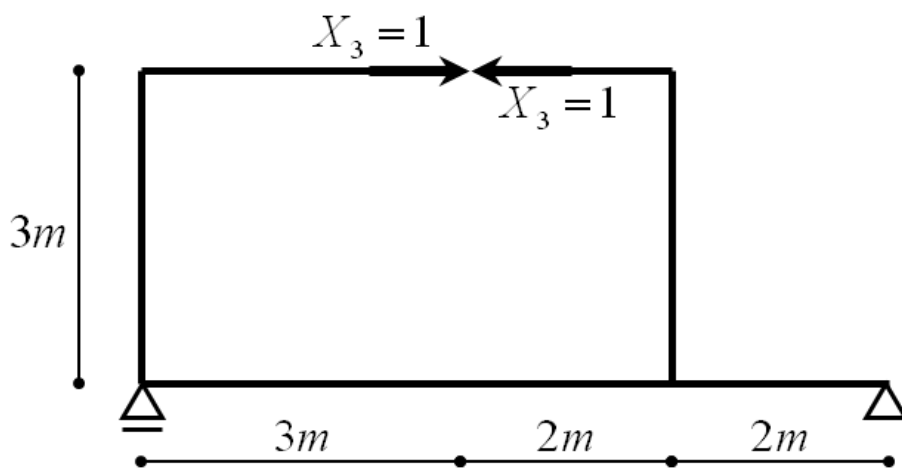
Reakcje w stanie  $X_2=1$



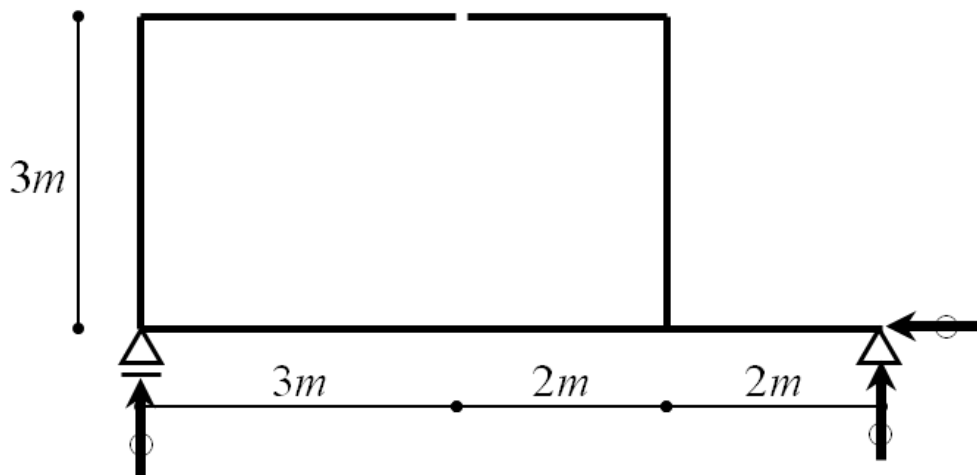


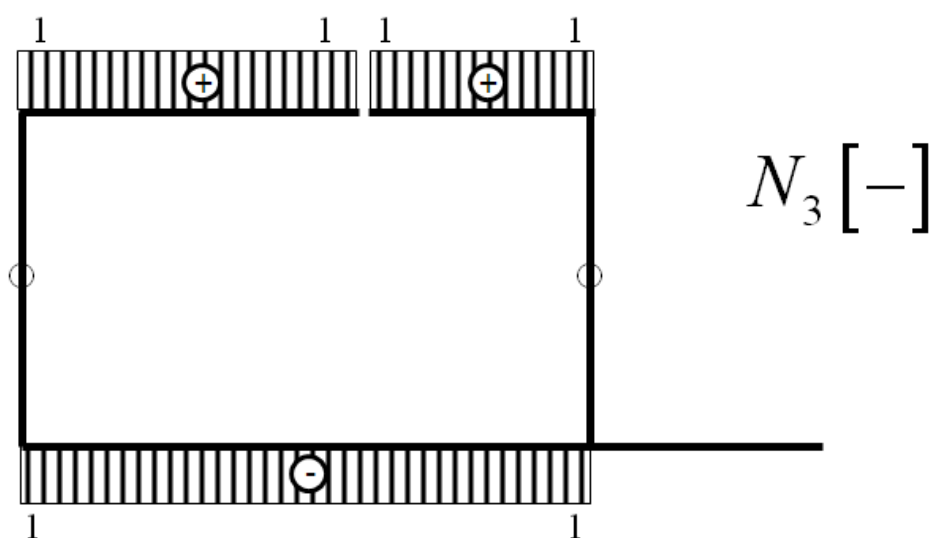
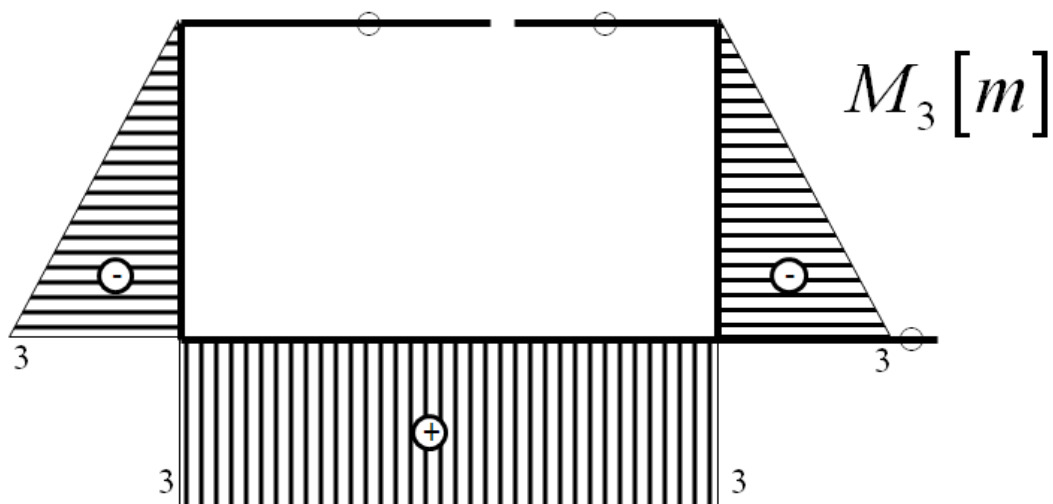
$$N_2 [-]$$

Stan  $X_3=1$



Reakcje w stanie  $X_3=1$





### Wyznaczenie współczynników układu równań

$$\delta_{11} = \frac{1}{E \cdot I_x} \left[ \begin{array}{c} \begin{array}{c} 7m \\ \text{+} \\ 1 \end{array} \\ \begin{array}{c} \text{+} \\ 1 \end{array} \end{array} \right]$$

$$\delta_{11} = \frac{1}{E \cdot I_x} \left( \frac{1}{2} \cdot 1 \cdot 7m \cdot \frac{2}{3} \cdot 1 \right) \quad \delta_{11} = 5.319 \times 10^{-4} \cdot \frac{1}{kN \cdot m} \quad E \cdot I_x \delta_{11} = 2.333 m$$

$$\delta_{22} = \frac{1}{E \cdot I_x} \left[ \begin{array}{c} \begin{array}{c} 3m \\ \text{-} \\ 3m \end{array} + \begin{array}{c} \text{-} \\ 3m \end{array} + \begin{array}{c} \text{-} \\ 3m \end{array} + \begin{array}{c} 3m \\ \text{+} \\ 3m \end{array} + \\ \begin{array}{c} 3m \\ \text{-} \\ 3m \end{array} + \begin{array}{c} \text{-} \\ 3m \end{array} + \begin{array}{c} \text{-} \\ 3m \end{array} + \begin{array}{c} 3m \\ \text{+} \\ 3m \end{array} + \\ \begin{array}{c} \text{+} \\ 2m \end{array} + \begin{array}{c} \text{+} \\ 2m \end{array} + \begin{array}{c} \text{+} \\ 3m \end{array} + \begin{array}{c} 2m \\ \text{+} \\ 2m \end{array} + \\ \begin{array}{c} \text{+} \\ 2m \end{array} + \begin{array}{c} \text{+} \\ 2m \end{array} + \begin{array}{c} \text{+} \\ 2m \end{array} + \begin{array}{c} 2m \\ \text{+} \\ 2m \end{array} + \end{array} \right]$$

$$\delta_{22} = \frac{1}{E \cdot I_x} \cdot \left( \frac{1}{2} \cdot 3 \cdot m \cdot 3 \cdot m \cdot \frac{2}{3} \cdot 3 \cdot m \cdot 2 + 3 \cdot m \cdot 3 \cdot m \cdot 3 \cdot m + \frac{1}{2} \cdot 2 \cdot m \cdot 2 \cdot m \cdot \frac{2}{3} \cdot 2m \cdot 2 + 2m \cdot 3m \cdot 2m \right)$$

$$\delta_{22} = 1.421 \times 10^{-2} \cdot \frac{m}{kN} \quad E \cdot I_x \delta_{22} = 62.333 \cdot m^3$$

$$\delta_{33} = \frac{1}{E \cdot I_x} \left[ \begin{array}{c} \left[ \begin{array}{c} \triangleleft \quad \triangleleft \\ 3m \quad 3m \end{array} \right] + \left[ \begin{array}{c} + \\ + \\ 5m \end{array} \right] + \left[ \begin{array}{c} \triangleleft \quad \triangleleft \\ 3m \quad 3m \end{array} \right] \end{array} \right]$$

$$\delta_{33} = \frac{1}{E \cdot I_x} \cdot \left( \frac{1}{2} \cdot 3 \cdot m \cdot 3 \cdot m \cdot \frac{2}{3} \cdot 3 \cdot m \cdot 2 + 3 \cdot m \cdot 5 \cdot m \cdot 3 \cdot m \right) \quad \delta_{33} = 1.436 \times 10^{-2} \cdot \frac{m}{kN} \quad E \cdot I_x \delta_{33} = 63 \cdot m^3$$

$$\delta_{12} = \frac{1}{E \cdot I_x} \left[ \begin{array}{c} \left[ \begin{array}{c} \triangleleft \quad + \\ 3m \quad 5m \end{array} \right] \end{array} \right]$$

$$\delta_{12} = \frac{1}{E \cdot I_x} \cdot \left[ \frac{1}{2} \cdot 0.714 \cdot 5 \cdot m \cdot \left[ \frac{2}{3} \cdot (-2 \cdot m) + \frac{1}{3} \cdot 3m \right] \right]$$

$$\delta_{12} = -1.356 \times 10^{-4} \cdot \frac{1}{kN} \quad E \cdot I_x \delta_{12} = -0.595 m^2$$

$$\delta_{21} = \delta_{12}$$

$$\delta_{13} = \frac{1}{E \cdot I_x} \left[ \begin{array}{c} \left[ \begin{array}{c} \triangleleft \quad + \\ 3m \quad 5m \end{array} \right] + \left[ \begin{array}{c} + \\ 3m \end{array} \right] \end{array} \right]$$

$$\delta_{13} = \frac{1}{E \cdot I_x} \cdot \left( \frac{1}{2} \cdot 5 \cdot m \cdot 0.714 \cdot 3m \right)$$

$$\delta_{13} = 1.221 \times 10^{-3} \cdot \frac{1}{kN} \quad E \cdot I_x \delta_{13} = 5.355 \cdot m^2$$

$$\delta_{31} = \delta_{13}$$

$$\delta_{23} = \frac{1}{E \cdot I_x} \left[ \begin{array}{c} \left[ \begin{array}{c} \square \quad \triangleleft \\ 3m \quad 3m \end{array} \right] + \left[ \begin{array}{c} \triangleleft \quad \triangleleft \\ 3m \quad 5m \end{array} \right] + \left[ \begin{array}{c} \square \quad \triangleleft \\ 2m \quad 3m \end{array} \right] \end{array} \right]$$

$$\delta_{23} = \frac{1}{E \cdot I_x} \cdot \left[ \frac{1}{2} \cdot 3 \cdot m \cdot (-3m) \cdot (-3m) + 5m \cdot 3m \cdot \frac{1}{2} [3m + (-2m)] + 2m \cdot 3m \cdot \frac{1}{2} \cdot (-3m) \right]$$

$$\delta_{23} = 2.735 \times 10^{-3} \cdot \frac{m}{kN} \quad E \cdot I_x \delta_{23} = 12 \cdot m^3$$

$$\delta_{32} = \delta_{23}$$

## Wyznaczenie wyrazów wolnych układu równań

$$\Delta_{1p} = \frac{1}{E \cdot I_x} \left[ \begin{array}{c} \begin{array}{c} \text{0,428} \\ \text{+} \\ \text{0,428} \end{array} \begin{array}{c} \text{+} \\ \text{0,714} \end{array} \begin{array}{c} \text{0,714} \\ \text{+} \\ \text{1} \end{array} \\ \begin{array}{c} \text{45} \\ \text{kNm} \end{array} \begin{array}{c} \text{+} \\ \text{3m} \end{array} \begin{array}{c} \text{57,703} \\ \text{kNm} \end{array} \\ \text{+} \begin{array}{c} \text{57,703} \\ \text{kNm} \end{array} \begin{array}{c} \text{+} \\ \text{2m} \end{array} \begin{array}{c} \text{48,852} \\ \text{kNm} \end{array} \\ \text{+} \begin{array}{c} \text{48,852} \\ \text{kNm} \end{array} \begin{array}{c} \text{+} \\ \text{2m} \end{array} \end{array} \right]$$

$$\Delta_{1p} = \frac{1}{E \cdot I_x} \left[ \frac{1}{2} \cdot 3m \cdot 0,428 \cdot \left( \frac{1}{3} \cdot 45kN \cdot m + \frac{2}{3} \cdot 57,703kN \cdot m \right) + \frac{1}{2} \cdot 0,428 \cdot 2m \cdot \left( \frac{2}{3} \cdot 57,703kN \cdot m + \frac{1}{3} \cdot 48,852kN \cdot m \right) \dots \right]$$

$$\left[ + \frac{1}{2} \cdot 0,714 \cdot 2m \cdot \left( \frac{1}{3} \cdot 57,703kN \cdot m + \frac{2}{3} \cdot 48,852kN \cdot m \right) + \frac{1}{2} \cdot 2m \cdot 48,852kN \cdot m \cdot \left( \frac{2}{3} \cdot 0,714 + \frac{1}{3} \cdot 1 \right) \right]$$

$$\Delta_{1p} = 3,061 \times 10^{-2}$$

$$E \cdot I_x \Delta_{1p} = 134,285 \cdot kN \cdot m^2$$

$$\Delta_{2p} = \frac{1}{E \cdot I_x} \left[ \begin{array}{c} \begin{array}{c} \text{45} \\ \text{kNm} \end{array} \begin{array}{c} \text{-} \\ \text{3m} \end{array} \begin{array}{c} \text{-} \\ \text{3m} \end{array} \\ \text{+} \begin{array}{c} \text{45} \\ \text{kNm} \end{array} \begin{array}{c} \text{-} \\ \text{3m} \end{array} \begin{array}{c} \text{-} \\ \text{3m} \end{array} \\ \text{+} \begin{array}{c} \text{45} \\ \text{kNm} \end{array} \begin{array}{c} \text{+} \\ \text{3m} \end{array} \begin{array}{c} \text{57,703} \\ \text{kNm} \end{array} \\ \text{+} \begin{array}{c} \text{57,703} \\ \text{kNm} \end{array} \begin{array}{c} \text{+} \\ \text{2m} \end{array} \begin{array}{c} \text{48,852} \\ \text{kNm} \end{array} \\ \text{+} \begin{array}{c} \text{20} \\ \text{kNm} \end{array} \begin{array}{c} \text{-} \\ \text{2m} \end{array} \begin{array}{c} \text{+} \\ \text{2m} \end{array} \\ \text{+} \begin{array}{c} \text{20} \\ \text{kNm} \end{array} \begin{array}{c} \text{+} \\ \text{2m} \end{array} \begin{array}{c} \text{-} \\ \text{2m} \end{array} \end{array} \right]$$

$$\Delta_{2p} = \frac{1}{E \cdot I_x} \left[ \frac{1}{3} (-45kN \cdot m) \cdot 3m \cdot \frac{3}{4} (-3m) + (-45kN \cdot m) \cdot 3m \cdot (-3m) + \frac{1}{2} \cdot 3m \cdot 3m \cdot \left( \frac{2}{3} \cdot 45kN \cdot m + \frac{1}{3} \cdot 57,703kN \cdot m \right) \dots \right]$$

$$\left[ + \frac{1}{2} \cdot 2m \cdot (-2m) \cdot \left( \frac{2}{3} \cdot 48,852kN \cdot m + \frac{1}{3} \cdot 57,703kN \cdot m \right) + (-20kN \cdot m) \cdot 2m \cdot 3m + \frac{1}{3} \cdot (-20kN \cdot m) \cdot 2m \cdot \frac{3}{4} \cdot 2m \right]$$

$$\Delta_{2p} = 1,104 \times 10^{-1} m$$

$$E \cdot I_x \Delta_{2p} = 484,2 \cdot kN \cdot m^3$$

$$\Delta_{3p} = \frac{1}{E \cdot I_x} \left[ \begin{array}{c} \begin{array}{c} \text{-} \\ \text{45 kNm} \end{array} \begin{array}{c} \text{-} \\ \text{3m} \end{array} \\ \text{+} \begin{array}{c} \text{45} \\ \text{kNm} \end{array} \begin{array}{c} \text{+} \\ \text{3m} \end{array} \begin{array}{c} \text{57,703} \\ \text{kNm} \end{array} \\ \text{+} \begin{array}{c} \text{57,703} \\ \text{kNm} \end{array} \begin{array}{c} \text{+} \\ \text{2m} \end{array} \begin{array}{c} \text{48,852} \\ \text{kNm} \end{array} \\ \text{+} \begin{array}{c} \text{20} \\ \text{kNm} \end{array} \begin{array}{c} \text{-} \\ \text{3m} \end{array} \begin{array}{c} \text{-} \\ \text{3m} \end{array} \\ \text{+} \begin{array}{c} \text{20} \\ \text{kNm} \end{array} \begin{array}{c} \text{-} \\ \text{3m} \end{array} \begin{array}{c} \text{-} \\ \text{3m} \end{array} \end{array} \right]$$

$$\Delta_{3p} = \frac{1}{E \cdot I_x} \left[ (-45 \cdot kN \cdot m) \cdot 3 \cdot m \cdot \frac{1}{2} \cdot (-3 \cdot m) + 3 \cdot m \cdot 3 \cdot m \cdot \frac{1}{2} \cdot (45 \cdot kN \cdot m + 57,703 \cdot kN \cdot m) \dots \right]$$

$$\left[ + 3 \cdot m \cdot 2 \cdot m \cdot \frac{1}{2} \cdot (48,852 \cdot kN \cdot m + 57,703 \cdot kN \cdot m) + 3 \cdot m \cdot (-20 \cdot kN \cdot m) \cdot \frac{1}{2} \cdot (-3 \cdot m) \right]$$

$$\Delta_{3p} = 2,449 \times 10^{-1} m$$

$$E \cdot I_x \Delta_{3p} = 1,074 \times 10^3 \cdot kN \cdot m^3$$



$$\Delta_{1\Delta} = -[0.143 \cdot (-0.01)] \quad \Delta_{1\Delta} = 1.43 \times 10^{-3}$$

$$\Delta_{2\Delta} = 0$$

$$\Delta_{3\Delta} = 0$$

$$\Delta_{1t0} = 0$$

$$\Delta_{2t0} = \alpha_t \cdot 10K \cdot (-1) \cdot 3m \quad \Delta_{2t0} = -3.6 \times 10^{-4} m$$

$$\Delta_{3t0} = \alpha_t \cdot 20K \cdot (-1) \cdot 5m \quad \Delta_{3t0} = -1.2 \times 10^{-3} m$$

$$\Delta_{1\Delta t} = \frac{\alpha_t}{h} \cdot 20K \cdot \frac{1}{2} \cdot 5m \cdot 0.714 \quad \Delta_{1\Delta t} = 2.142 \times 10^{-3} \quad \Delta_{1\Delta t} = 2.142 \times 10^{-3}$$

$$\Delta_{2\Delta t} = \frac{\alpha_t}{h} \cdot 20K \cdot \left[ \frac{1}{2} \cdot 3m \cdot 3m + \frac{1}{2} \cdot 2m \cdot (-2m) \right] \quad \Delta_{2\Delta t} = 3 \times 10^{-3} m$$

$$\Delta_{3\Delta t} = \frac{\alpha_t}{h} \cdot 20K \cdot 3m \cdot 5m \quad \Delta_{3\Delta t} = 0.018 m$$

$$\Delta_{10} = \Delta_{1p} + (\Delta_{1\Delta} + \Delta_{1t0} + \Delta_{1\Delta t}) \quad \Delta_{10} = 0.034$$

$$\Delta_{20} = \Delta_{2p} + (\Delta_{2\Delta} + \Delta_{2t0} + \Delta_{2\Delta t}) \quad \Delta_{20} = 0.113 m$$

$$\Delta_{30} = \Delta_{3p} + (\Delta_{3\Delta} + \Delta_{3t0} + \Delta_{3\Delta t}) \quad \Delta_{30} = 0.262 m$$

### Z podporą sprężystą

$$V_{Ap} = 24.426 kN \quad V_{A1} = -0.143 \cdot \frac{1}{m} \quad V_{A2} = 0 \quad V_{A3} = 0 \quad K_y = 250 \frac{kN}{m}$$

$$\delta_{11} = 5.319 \times 10^{-4} \cdot \frac{1}{kN \cdot m} \quad \frac{V_{A1} \cdot V_{A1}}{K_y} = 8.18 \times 10^{-5} \cdot \frac{1}{kN \cdot m} \quad \delta_{11} = \delta_{11} + \frac{V_{A1} \cdot V_{A1}}{K_y} = 6.137 \times 10^{-4} \cdot \frac{1}{kN \cdot m}$$

$$\delta_{22} = 1.421 \times 10^{-2} \cdot \frac{m}{kN} \quad \frac{V_{A2} \cdot V_{A2}}{K_y} = 0 \quad \delta_{22} = \delta_{22} + \frac{V_{A2} \cdot V_{A2}}{K_y} = 1.421 \times 10^{-2} \cdot \frac{m}{kN}$$

$$\delta_{33} = 1.436 \times 10^{-2} \cdot \frac{m}{kN} \quad \frac{V_{A3} \cdot V_{A3}}{K_y} = 0 \quad \delta_{33} = \delta_{33} + \frac{V_{A3} \cdot V_{A3}}{K_y} = 1.436 \times 10^{-2} \cdot \frac{m}{kN}$$

$$\delta_{12} = -1.356 \times 10^{-4} \cdot \frac{1}{kN} \quad \frac{V_{A1} \cdot V_{A2}}{K_y} = 0 \quad \delta_{12} = \delta_{12} + \frac{V_{A1} \cdot V_{A2}}{K_y} = -1.356 \times 10^{-4} \cdot \frac{1}{kN} \quad \delta_{21} = \delta_{12}$$

$$\delta_{13} = 1.221 \times 10^{-3} \cdot \frac{1}{m} \cdot \frac{m}{kN} \quad \frac{V_{A1} \cdot V_{A3}}{K_y} = 0 \quad \delta_{13} = \delta_{13} + \frac{V_{A1} \cdot V_{A3}}{K_y} = 1.221 \times 10^{-3} \cdot \frac{1}{m} \cdot \frac{m}{kN} \quad \delta_{31} = \delta_{13}$$

$$\delta_{23} = 2.735 \times 10^{-3} \cdot \frac{m}{kN} \quad \frac{V_{A2} \cdot V_{A3}}{K_y} = 0 \quad \delta_{23} = \delta_{23} + \frac{V_{A2} \cdot V_{A3}}{K_y} = 2.735 \times 10^{-3} \cdot \frac{m}{kN} \quad \delta_{32} = \delta_{23}$$

$$\begin{aligned} \Delta_{10} &= 3.418 \times 10^{-2} & \frac{V_{A1'} \cdot V_{Ap}}{K_y} &= -1.397 \times 10^{-2} & \Delta_{10} &= \Delta_{10} + \frac{V_{A1'} \cdot V_{Ap}}{K_y} = 2.021 \times 10^{-2} \\ \Delta_{20} &= 1.13 \times 10^{-1} \text{ m} & \frac{V_{A2'} \cdot V_{Ap}}{K_y} &= 0 \times 10^0 & \Delta_{20} &= \Delta_{20} + \frac{V_{A2'} \cdot V_{Ap}}{K_y} = 1.13 \times 10^{-1} \text{ m} \\ \Delta_{30} &= 2.617 \times 10^{-1} \text{ m} & \frac{V_{A3'} \cdot V_{Ap}}{K_y} &= 0 \times 10^0 & \Delta_{30} &= \Delta_{30} + \frac{V_{A3'} \cdot V_{Ap}}{K_y} = 2.617 \times 10^{-1} \text{ m} \end{aligned}$$

## Rozwiązanie układu równań

$$\delta_{11'} \cdot X_1 + \delta_{12'} \cdot X_2 + \delta_{13'} \cdot X_3 + \Delta_{10} = 0.01$$

$$\delta_{21'} \cdot X_1 + \delta_{22'} \cdot X_2 + \delta_{23'} \cdot X_3 + \Delta_{20} = 0$$

$$\delta_{31'} \cdot X_1 + \delta_{32'} \cdot X_2 + \delta_{33'} \cdot X_3 + \Delta_{30} = 0$$

$$X_1 = 20.668 \cdot \text{kN} \cdot \text{m} \quad X_2 = -4.059 \cdot \text{kN} \quad X_3 = -19.206 \cdot \text{kN}$$

<b>X1</b>	20,668				
<b>X2</b>	-4,059				
<b>X3</b>	-19,206				
	<b>Mp</b>	<b>M1</b>	<b>M2</b>	<b>M3</b>	<b>Most</b>
<b>AD</b>	0	1	0	0	<b>20,668</b>
<b>DA</b>	48,852	0,714	0	0	<b>63,609</b>
<b>DC</b>	48,852	0,714	-2	3	<b>14,109</b>
<b>DG</b>	-20	0	2	-3	<b>29,500</b>
<b>CD</b>	57,703	0,428	0	3	<b>8,931</b>
<b>CB</b>	57,703	0,428	0	3	<b>8,931</b>
<b>BC</b>	45	0	3	3	<b>-24,795</b>
<b>BE</b>	-45	0	-3	-3	<b>24,795</b>
<b>EB</b>	-45	0	-3	0	<b>-32,823</b>
<b>EF</b>	-45	0	-3	0	<b>-32,823</b>
<b>FE</b>	0	0	0	0	<b>0,000</b>
<b>FG</b>	0	0	0	0	<b>0,000</b>
<b>GF</b>	-20	0	2	0	<b>-28,118</b>
<b>GD</b>	-20	0	2	0	<b>-28,118</b>

### Sprawdzenie równowagi momentów w węzłach

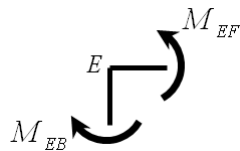


Diagram of node E showing moments  $M_{EB}$  and  $M_{EF}$ .

$$M_{EB} - M_{EF} = 0 \cdot kN \cdot m$$

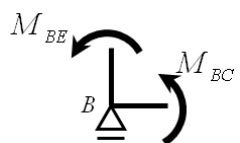


Diagram of node B showing moments  $M_{BE}$  and  $M_{BC}$ .

$$M_{BE} + M_{BC} = 0 \cdot kN \cdot m$$

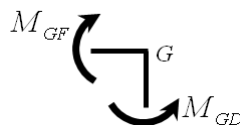


Diagram of node G showing moments  $M_{GF}$  and  $M_{GD}$ .

$$M_{GF} - M_{GD} = 0 \cdot kN \cdot m$$

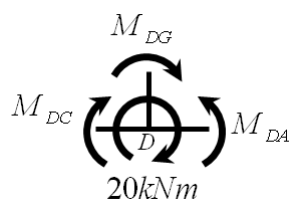
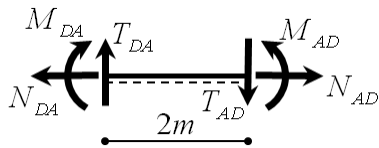


Diagram of node D showing moments  $M_{DC}$ ,  $M_{DG}$ , and  $M_{DA}$ , with an external moment of  $20kNm$ .

$$M_{DC} + M_{DG} - M_{DA} + 20kN \cdot m = 0 \cdot kN \cdot m$$

## Wyznaczenie sił tnących

### Pręt DA



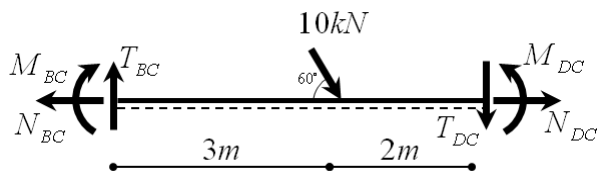
$$\Sigma M_A = 0$$

$$T_{DA} \cdot 2m + M_{DA} - M_{AD} = 0$$

$$\Sigma Y = 0 \quad T_{AD} = T_{DA}$$

$$T_{DA} = -21.471 \cdot kN \quad T_{AD} = -21.471 \cdot kN$$

### Pręt BD



$$\Sigma M_C = 0$$

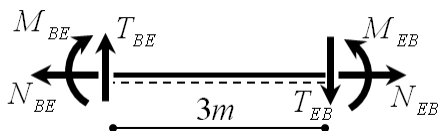
$$T_{BC} \cdot 5m + M_{BC} - M_{DC} - 10kN \cdot \sin(60deg) \cdot 2m = 0$$

$$\Sigma Y = 0$$

$$T_{BC} - T_{DC} - 10kN \cdot \sin(60deg) = 0$$

$$T_{DC} = 2.585 \cdot kN \quad T_{BC} = 11.245 \cdot kN$$

### Pręt BE



$$\Sigma M_E = 0$$

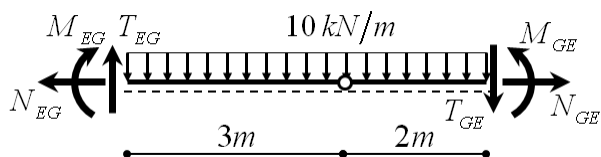
$$T_{BE} \cdot 3m + M_{BE} - M_{EB} = 0$$

$$\Sigma Y = 0$$

$$T_{EB} = T_{BE}$$

$$T_{BE} = -19.206 \cdot kN \quad T_{EB} = -19.206 \cdot kN$$

### Pręt EG



$$\Sigma M_G = 0$$

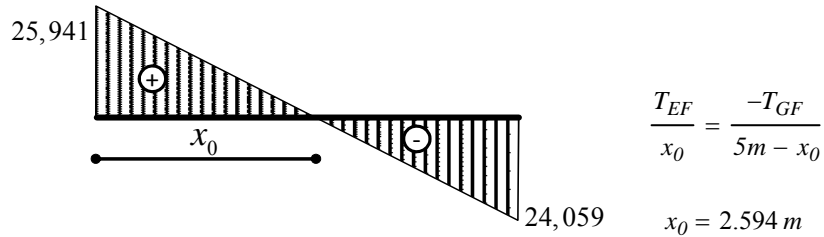
$$T_{EF} \cdot 5m + M_{EF} - M_{GF} - 10 \frac{kN}{m} \cdot 5m \cdot \frac{5m}{2} = 0$$

$$\Sigma Y = 0$$

$$T_{EF} - T_{GF} - 10 \frac{kN}{m} \cdot 5m = 0$$

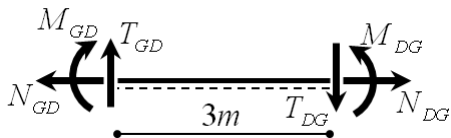
$$T_{GF} = -24.059 \cdot kN \quad T_{EF} = 25.941 \cdot kN$$

### Wyznaczenie maksymalnego momentu



$$M_{max} = M_{EF} + T_{EF} \cdot x_0 - 10 \frac{kN}{m} \cdot x_0 \cdot \frac{x_0}{2} \quad M_{max} = 0.824 \cdot kN \cdot m$$

### Pręt GD



$$\Sigma M_D = 0$$

$$T_{GD} \cdot 3m + M_{GD} - M_{DG} = 0$$

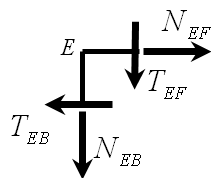
$$\Sigma Y = 0$$

$$T_{DG} = T_{GD}$$

$$T_{GD} = 19.206 \cdot kN \quad T_{DG} = 19.206 \cdot kN$$

## Równowaga węzłów - siły normalne i reakcje

### Węzeł E



$$\Sigma X = 0 \quad N_{EF} - T_{EB} = 0$$

$$N_{EF} = -19.206 \cdot kN$$

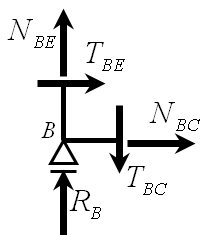
$$\Sigma Y = 0$$

$$N_{EB} + T_{EF} = 0$$

$$N_{EB} = -25.941 \cdot kN$$

$$N_{GF} = N_{EF} \quad N_{BE} = N_{EB} \quad (\text{z warunków równowagi prętów EG i BE})$$

### Węzeł B



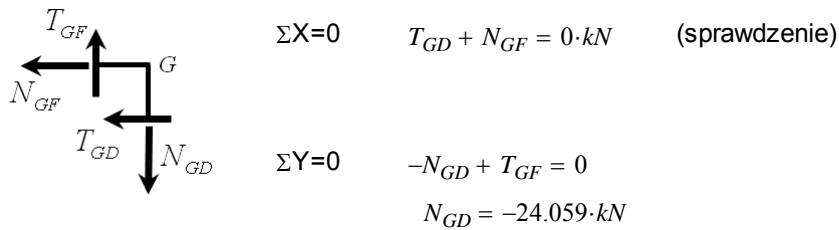
$$\Sigma X = 0 \quad N_{BC} + T_{BE} = 0$$

$$N_{BC} = 19.206 \cdot kN$$

$$\Sigma Y = 0 \quad N_{BE} + R_B - T_{BC} = 0$$

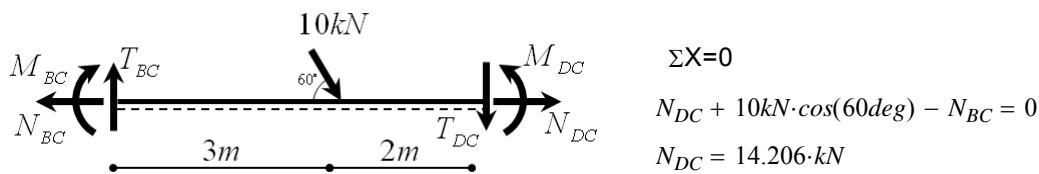
$$R_B = 37.186 \cdot kN$$

### Węzeł G

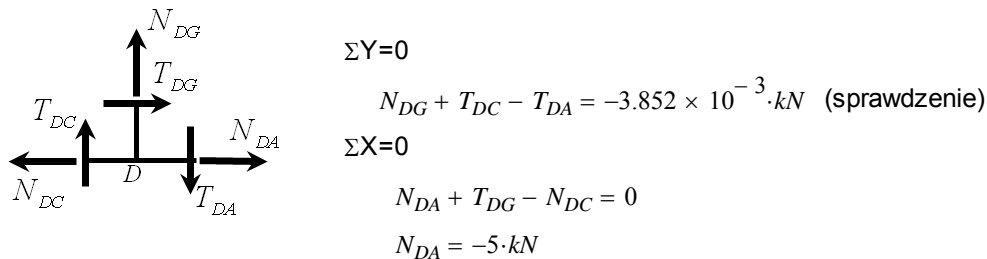


$N_{DG} = N_{GD}$  (z warunku równowagi pręta DG)

### Pręt BD

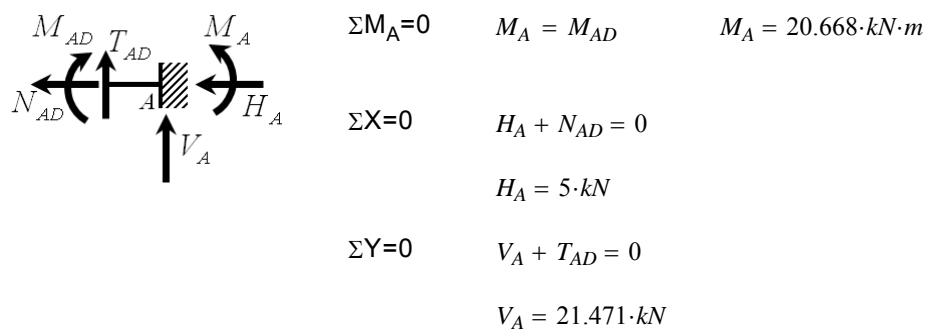


### Węzeł D

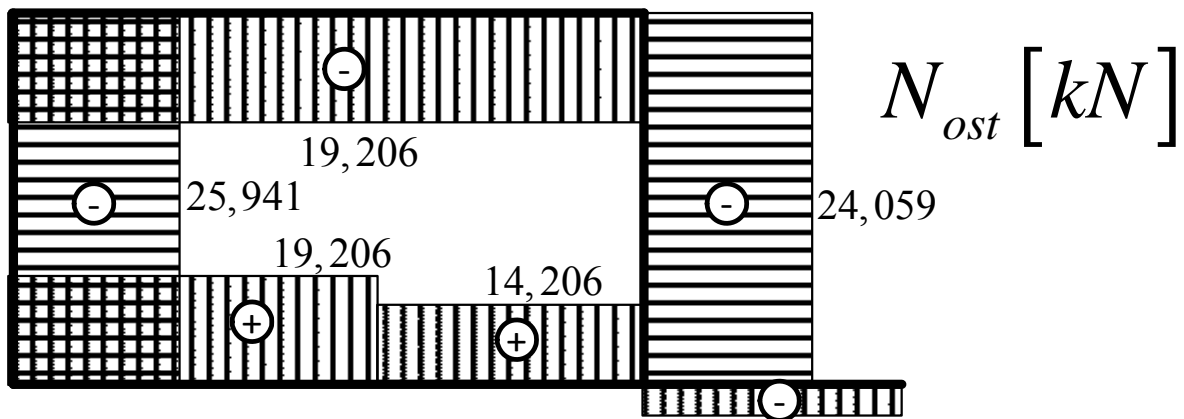
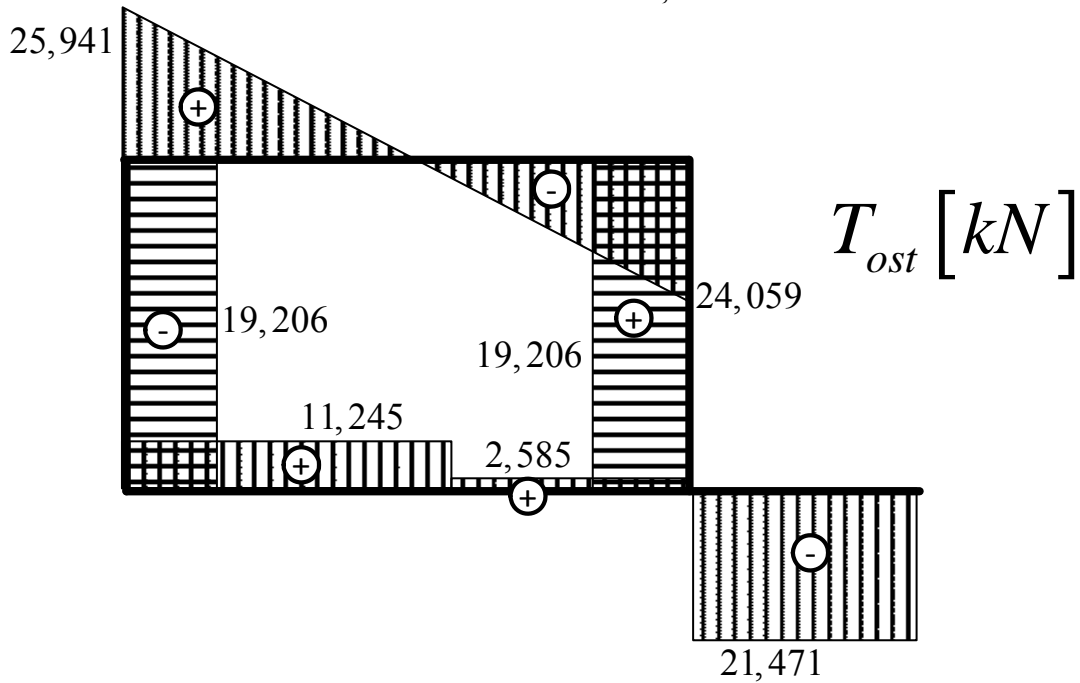
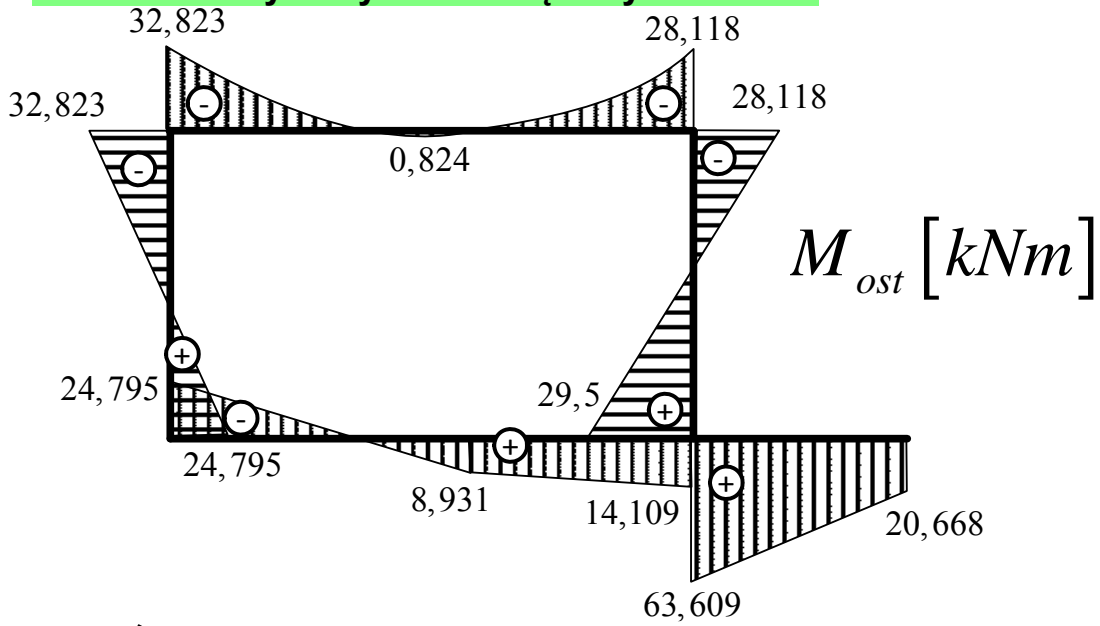


$N_{AD} = N_{DA}$  (z warunku równowagi pręta DA)

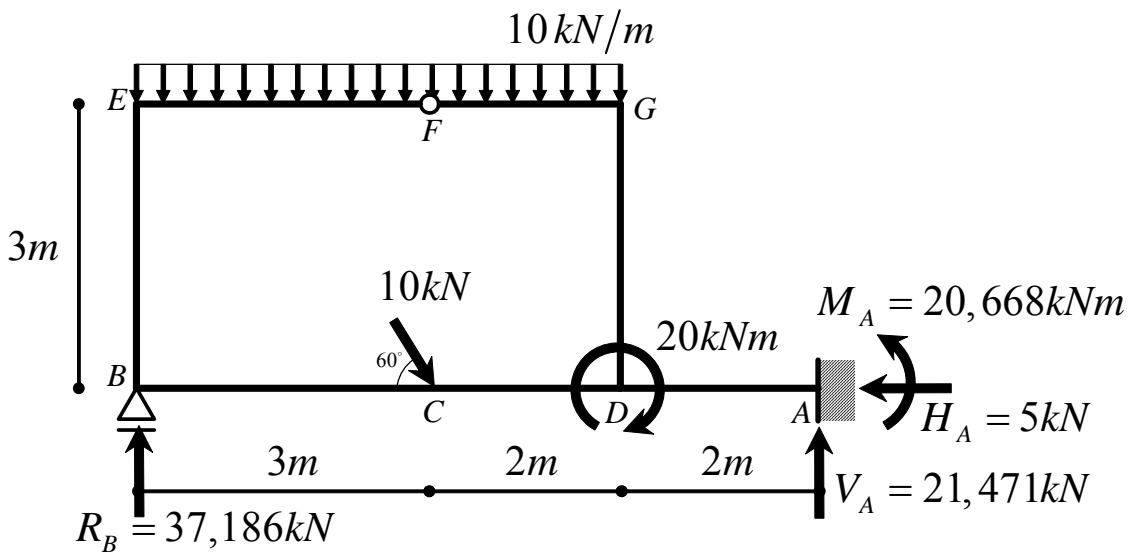
### Węzeł A



## Ostateczne wykresy sił wewnętrznych



## Sprawdzenia statyczne



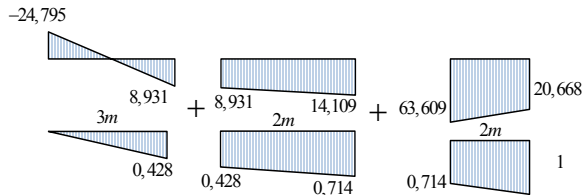
$$\Sigma X=0 \quad -H_A + 10kN \cdot \cos(60deg) = 0 \cdot kN$$

$$\Sigma Y=0 \quad R_B + V_A - 10kN \sin(60deg) - 10 \frac{kN}{m} \cdot 5m = -3.852 \times 10^{-3} \cdot kN$$

$$\Sigma M_G=0 \quad R_B \cdot 5m - 10 \frac{kN}{m} \cdot 5m \cdot \frac{5m}{2} - 10kN \cdot \sin(60deg) \cdot 2m - 10kN \cdot \cos(60deg) \cdot 3m \dots = 1.091 \times 10^{-14} \cdot kN \cdot m$$

$$+ 20kN \cdot m - V_A \cdot 2m + H_A \cdot 3m - M_A$$

## Sprawdzenie kinematyczne



$$\varphi_{1p} = \frac{1}{E \cdot I_x} \left[ \frac{1}{2} \cdot 3m \cdot 0.428 \cdot \left( \frac{1}{3} \cdot M_{BC} + \frac{2}{3} \cdot M_{CB} \right) \dots \right.$$

$$\left. + \frac{1}{2} \cdot 2m \cdot M_{CD} \cdot \left( \frac{2}{3} \cdot 0.428 + \frac{1}{3} \cdot 0.714 \right) + \frac{1}{2} \cdot 2m \cdot M_{DC} \cdot \left( \frac{1}{3} \cdot 0.428 + \frac{2}{3} \cdot 0.714 \right) \dots \right.$$

$$\left. + \frac{1}{2} \cdot 2m \cdot M_{DA} \cdot \left( \frac{2}{3} \cdot 0.714 + \frac{1}{3} \cdot 1 \right) + \frac{1}{2} \cdot 2m \cdot M_{AD} \cdot \left( \frac{1}{3} \cdot 0.714 + \frac{2}{3} \cdot 1 \right) \right]$$

$$\varphi_{1p} = 1.871 \times 10^{-2}$$

$$\varphi_{1t} = \Delta_{I\Delta t} \quad \varphi_{1t} = 2.142 \times 10^{-3}$$

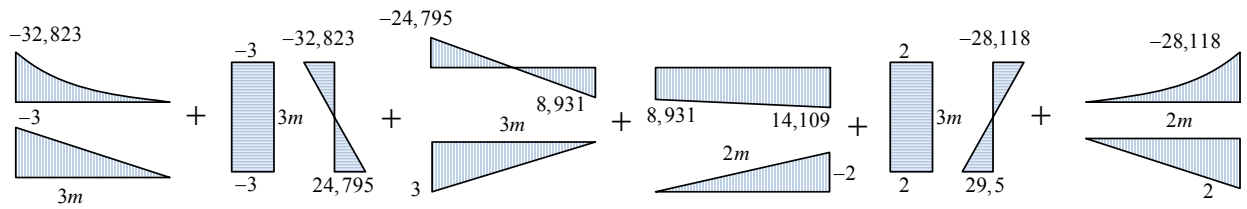
$$\varphi_{1\Delta} = -(1 \cdot 0.01 - 0.143 \cdot 0.01) \quad \varphi_{1\Delta} = -8.57 \times 10^{-3}$$

$$\varphi_{1k} = \frac{V_{A1} \cdot V_A}{K_y} \quad \varphi_{1k} = -0.012$$

$$\varphi_1 = \varphi_{1p} + \varphi_{1t} + \varphi_{1\Delta} + \varphi_{1k} \quad \varphi_1 = 4.695 \times 10^{-6}$$

$$\Delta = \frac{\varphi_1}{\varphi_{1p}} \quad \Delta = 0.025 \cdot \%$$





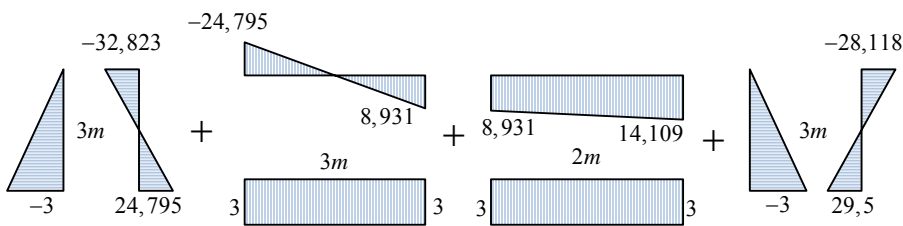
$$\Delta_{2ost} = \frac{1}{E \cdot I_x} \left[ \begin{aligned} & \frac{1}{2} \cdot 3m \cdot (-3m) \cdot \frac{2}{3} \cdot (-32.823kN \cdot m) + \frac{2}{3} \cdot \frac{10 \frac{kN}{m} \cdot (3m)^2}{8} \cdot 3m \cdot \frac{1}{2} \cdot (-3m) \dots \\ & + 3m \cdot (-3m) \cdot \left[ \frac{1}{2} \cdot (-32.823kN \cdot m) + \frac{1}{2} \cdot 24.795kN \cdot m \right] + \frac{1}{2} \cdot 3m \cdot 3m \cdot \left[ \frac{2}{3} \cdot (-24.795kN \cdot m) + \frac{1}{3} \cdot 8.931kN \cdot m \right] \dots \\ & + \frac{1}{2} \cdot 2m \cdot (-2m) \cdot \left( \frac{1}{3} \cdot 8.931kN \cdot m + \frac{2}{3} \cdot 14.109kN \cdot m \right) + 2m \cdot 3m \cdot \left[ \frac{1}{2} \cdot 29.5 \cdot kN \cdot m + \frac{1}{2} \cdot (-28.118kN \cdot m) \right] \dots \\ & + \frac{1}{2} \cdot 2m \cdot 2m \cdot \frac{2}{3} \cdot (-28.118kN \cdot m) + \frac{2}{3} \cdot \frac{10 \frac{kN}{m} \cdot (2m)^2}{8} \cdot 2m \cdot \frac{1}{2} \cdot 2m \end{aligned} \right]$$

$$\Delta_{2ost} = -2.641 \times 10^{-3} m$$

$$\Delta_{2t} = \Delta_{2\Delta t} + \Delta_{2t0} = 2.64 \times 10^{-3} m \quad \Delta_{2\Delta} = 0 \quad \Delta_{2k} = \frac{V_{A2} \cdot V_A}{K_y} = 0$$

$$\Delta_2 = \Delta_{2ost} + \Delta_{2t} + \Delta_{2\Delta} + \Delta_{2k} = -1.327 \times 10^{-6} m$$

$$\Delta = \frac{\Delta_2}{\Delta_{2ost}} \quad \Delta = 0.05\%$$



$$\Delta_{3ost} = \frac{1}{E \cdot I_x} \left[ \begin{aligned} & \frac{1}{2} \cdot 3m \cdot (-3m) \cdot \left[ \frac{1}{3} \cdot (-32.823kN \cdot m) + \frac{2}{3} \cdot 24.795kN \cdot m \right] + 3m \cdot 3m \cdot \left[ \frac{1}{2} \cdot (-24.795kN \cdot m) + \frac{1}{2} \cdot 8.931kN \cdot m \right] \dots \\ & + 3m \cdot 2m \cdot \left( \frac{1}{2} \cdot 8.931kN \cdot m + \frac{1}{2} \cdot 14.109kN \cdot m \right) + \frac{1}{2} \cdot 3m \cdot (-3m) \cdot \left[ \frac{2}{3} \cdot 29.5 \cdot kN \cdot m + \frac{1}{3} \cdot (-28.118kN \cdot m) \right] \end{aligned} \right]$$

$$\Delta_{3ost} = -1.681 \times 10^{-2} m$$

$$\Delta_{3t} = \Delta_{3\Delta t} + \Delta_{3t0} = 1.68 \times 10^{-2} m$$

$$\Delta_{3\Delta} = 0$$

$$\Delta_{3k} = \frac{V_{A3} \cdot V_A}{K_y} = 0$$

$$\Delta_3 = \Delta_{3ost} + \Delta_{3t} + \Delta_{3\Delta} + \Delta_{3k} = -9.095 \times 10^{-6} m$$

$$\Delta = \frac{\Delta_3}{\Delta_{3ost}} \quad \Delta = 0.054\%$$